

# Evaluating Spatial Pricing in Ride-Sourcing Systems

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# Introduction

*Ride-sourcing companies or TNCs, provide pre-arranged or on-demand transportation service for compensation.*

## Background

From **drivers** perspective, trips may be mispriced relative to other trip opportunities, leading to inefficiencies on a network level:

- Loss of service reliability
- Limit long-term driver participation

Recent research efforts have addressed ride-sourcings spatial mispricing problem with the objective of reducing *search frictions*<sup>1</sup> using:

- Spatial surge pricing models
- Spatio-temporal pricing mechanisms
- Search and matching models
- Non-linear pricing models

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<sup>1</sup>Imbalance between driver supply and passenger demand across geographic areas that causes the presence of high matching and reaching times.

# Introduction

## Motivation

- Methods focused on the optimization of the platform revenue and do not evaluate the driver perspective
- Limited evidence on the driver opportunity cost of the trip destination
- Lack of understanding of the spatial structure of driver productivity<sup>2</sup>
- Limited empirical evaluations

## Objective

Analyze the spatial structure of ride-sourcing operational and driver performance variables to support the need for new pricing strategies.

*We explore the spatial structure of ride-sourcing search frictions and driver performance variables as a function of the trip destination.*

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<sup>2</sup>We define the driver productivity in terms of profit per unit time.

# Introduction

Analyzing operational and performance variables at a high-definition spatial level requires additional data analytics methods. We propose the use of a spatial smoothing or denoising technique that:

- Allows fine resolution analysis
- Compensates for inherent sampling noise
- Enhances interpretability

## Contributions

- 1 Empirical evidence of spatial and temporal variation of driver productivity variables as a function of trip destination.
- 2 Temporal and spatial evaluation of different ride-sourcing operational measures and search frictions in Austin.
- 3 Implementation of a spatial denoising methodology to analyze high-definition spatial variables.

# Methodology

## Ride-Sourcing Data

Austin-based TNC (Ride Austin) trips<sup>3</sup> during the period that Uber and Lyft were out of the city.

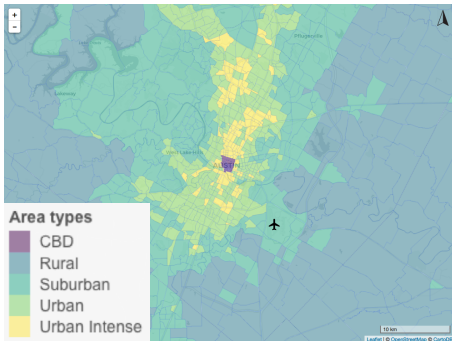
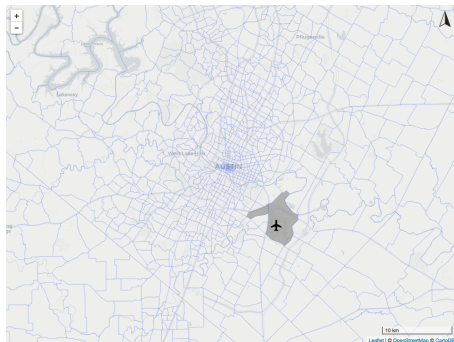
- Space discretization
  - ▶ Data is summarized over 1,305 traffic analysis zones (TAZs)
  - ▶ TAZ areas vary from 0.01  $km^2$  in the Central Business District (CBD) to 30  $km^2$  in the rural area, with an average of 2  $km^2$
- Time discretization
  - ▶ Weekday AM-peak
  - ▶ Weekday PM-peak
  - ▶ Weekday off-peak
  - ▶ Weekend

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<sup>3</sup><https://data.world/ride-austin>

# Methodology

## Ride-Sourcing Data



(a) TAZs in Austin (airport shaded)

(b) TAZ area types

Figure: Description of TAZs

# Methodology

## Ride-Sourcing Data

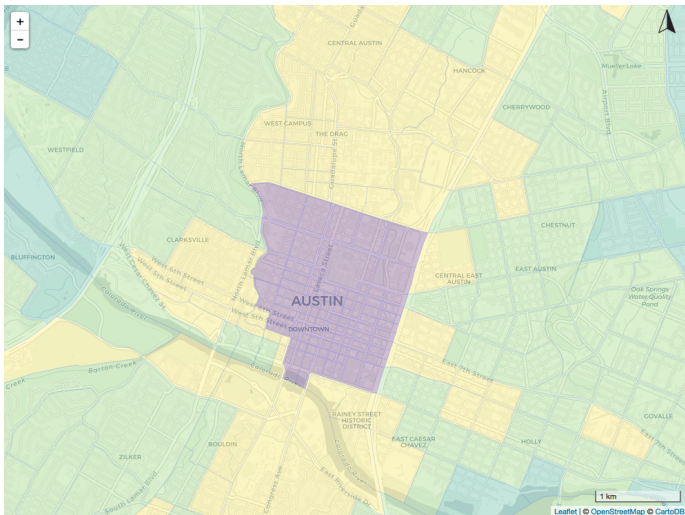


Figure: TAZ area types (downtown)



# Methodology

## Description of variables

- Operational (based on trip origin)

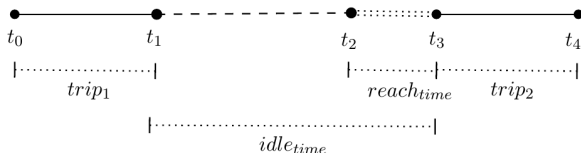


Figure: Driver time diagram

- Productivity, CBD-origin trips only (based on trip destination)

$$\text{Productivity } \mathbf{A} = \frac{\text{fare}_{\text{trip}_1}}{t_1} \quad (1)$$

$$\text{Productivity } \mathbf{B} = \frac{\text{fare}_{\text{trip}_1}}{t_3} \quad (2)$$

$$\text{Productivity } \mathbf{C} = \frac{\text{fare}_{\text{trip}_1} + \text{fare}_{\text{trip}_2}}{t_4} \quad (3)$$

# Spatial Smoothing Approach

## Background

- Typically used for a wide range of applications:
  - ▶ Predicting crime hotspots
  - ▶ Detecting crash hotspots
  - ▶ Special event detection
- Approaches types:
  - ▶ **Local**
    - Smooth only a local window around each point.
    - *Gaussian* smoothing, average a point over its neighboring values, thus removing noise by blurring.
  - ▶ **Global**
    - Define an objective function over the entire graph and simultaneously optimize the whole set of points.
    - *Total variation denoising or fused lasso*, removes noise by emphasizing edges.

# Spatial Smoothing Approach

## Smoothing

Assume that we have observations  $y_i$ , each associated with a vertex  $s_i \in \mathcal{V}$  in an undirected graph  $\mathcal{G} = (\mathcal{V}, \mathcal{E})$  with node set  $\mathcal{V}$  and edge set  $\mathcal{E}$ .

$$y_i = x_i + \epsilon_i, \quad i = 1, \dots, n, \quad (4)$$

where,  $x_i$  is the “true” denoised signal and  $\epsilon_i$  is mean-zero error.

*The goal of the smoothing techniques is to estimate  $x_i$  in a way that leverages the assumption of spatial smoothness over the underlying graph.*

# Spatial Smoothing Approach

## Graph-Fused Lasso

One way to estimate  $x$  is by using the GFL, defined by a convex optimization problem that penalizes the first differences of the signal across edges.

$$\underset{x \in \mathbb{R}^n}{\text{minimize}} \quad \ell(\mathbf{y}, \mathbf{x}) + \lambda \sum_{(r,s) \in \mathcal{E}} |x_r - x_s|, \quad (5)$$

where,  $\ell$  is the loss function,  $r$  is the start node and  $s$  the end node,  $n = |\mathcal{V}|$ , and  $\lambda > 0$  is the regularization parameter.

- Equation 5 does not have a closed-form solution. Convex optimization approaches are required.
- We implemented the method developed by Tansey and Scott (2015)<sup>4</sup>, which leads to an efficient approach that presents a fast and scalable solution.

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<sup>4</sup>Tansey, W., & Scott, J. G. (2015). A fast and flexible algorithm for the graph-fused lasso. arXiv preprint arXiv:1505.06475.

# Spatial Smoothing Approach

## Loss Function

Penalized weighted least squared-error loss function to take into account the differences in the number of observations within each zone.

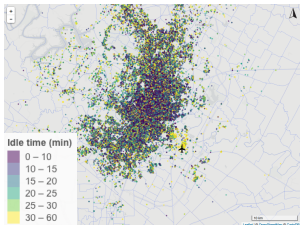
$$\underset{\mathbf{x} \in \mathbb{R}^n}{\text{minimize}} \quad \sum_{i=1}^n \frac{\eta_i}{2} (y_i - x_i)^2 + \lambda \sum_{(r,s) \in \mathcal{E}} |x_r - x_s| \quad (6)$$

Where,  $\eta_i$  is the count of trips observed within the  $i$ -th TAZ.

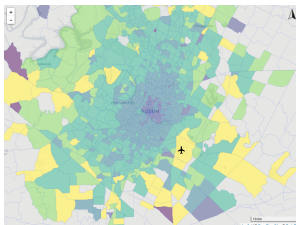
## Choosing the Regularization Parameter

- Split the data into a training and a test set
- Estimate the out-of-sample prediction error using the root mean square error (RMSE) criterion

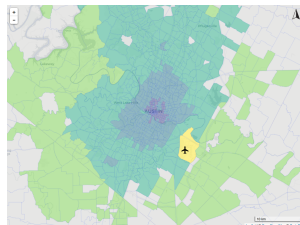
# Spatial Smoothing Approach



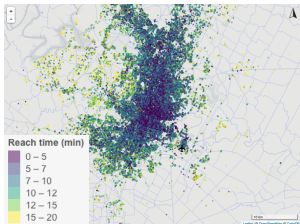
(a) Idle time data



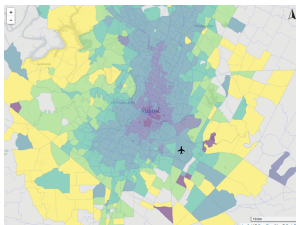
(b) Non-smoothed



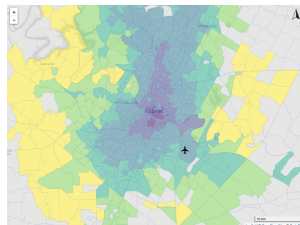
(c) Smoothed



(d) Reach time data



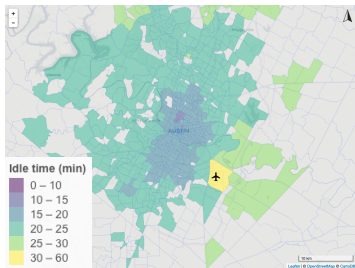
(e) Non-smoothed



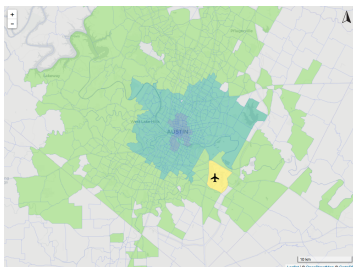
(f) Smoothed

Figure: GFL denoising example

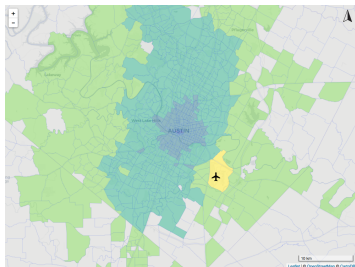
# Results - Operational Variables



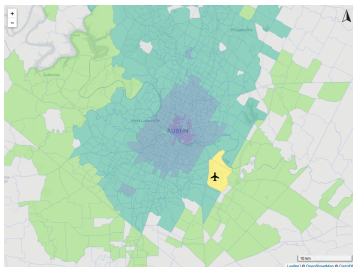
(a) Idle time AM-peak



(b) Idle time PM-peak

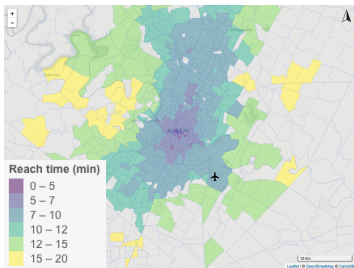


(c) Idle time off-peak

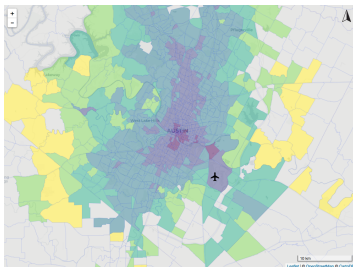


(d) Idle time weekend

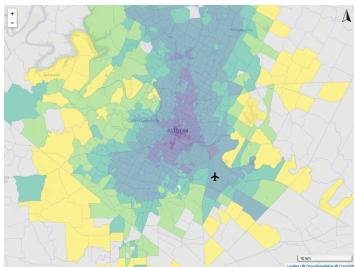
# Results - Operational Variables



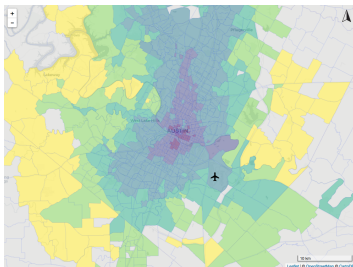
(a) Reach time AM-peak



(b) Reach time PM-peak



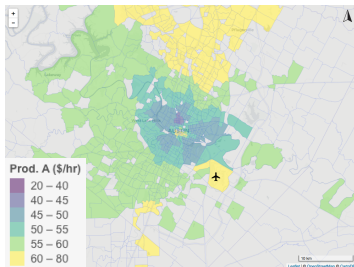
(c) Reach time off-peak



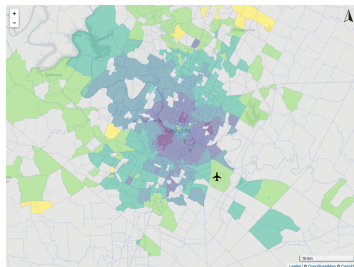
(d) Reach time weekend



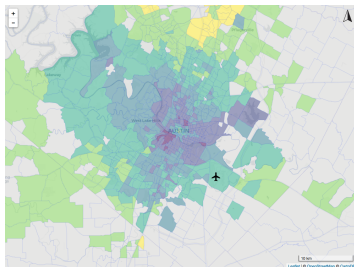
# Results - Productivity Variables



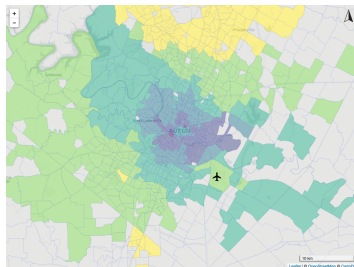
(a) Prod. A AM-peak



(b) Prod. A PM-peak

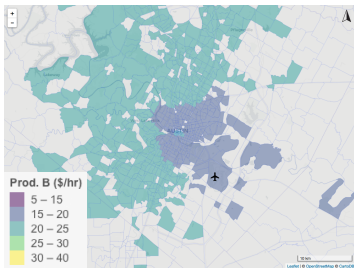


(c) Prod. A off-peak

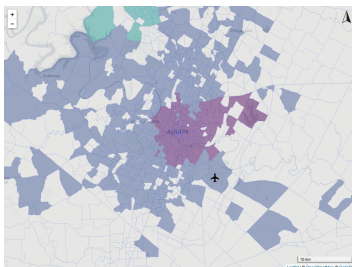


(d) Prod. A weekend

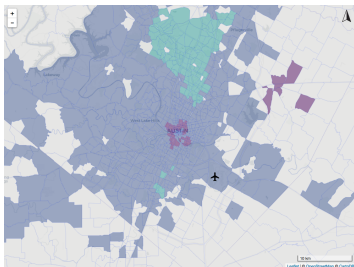
# Results - Productivity Variables



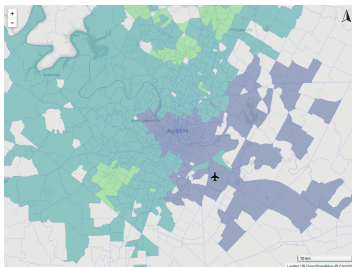
(a) Prod. B AM-peak



(b) Prod. B PM-peak

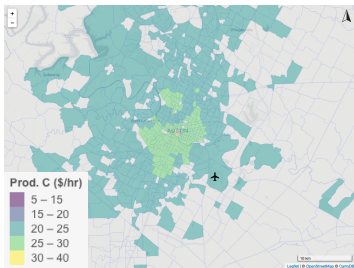


(c) Prod. B off-peak

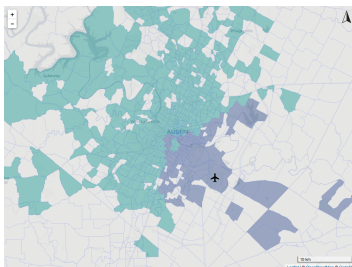


(d) Prod. B weekend

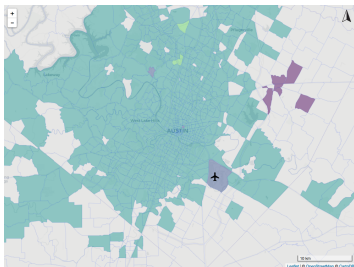
# Results - Productivity Variables



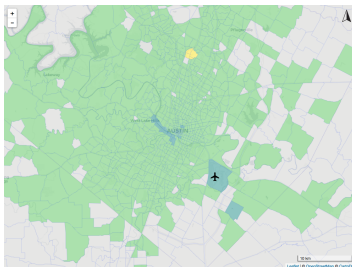
(a) Prod. C AM-peak



(b) Prod. C PM-peak



(c) Prod. C off-peak



(d) Prod. C weekend

# Conclusions

*Primary findings of this research suggest that there are differences in space and time that can affect ride-sourcing search frictions and driver productivity. Providing spatio-temporal pricing strategies could be one way to balance driver equity across the network.*

- **Driver and operator point of view**  
More efficient driver supply method.
- **Planners and engineers perspective**  
Understand the characteristics of of the ride-sourcing service in Austin.
- **Pricing strategies and policies**  
Warranty fair conditions in driver compensation.

# Thanks!

Questions or Comments?  
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